

### Math Circle Problems for week 6

1. Please see problem 6 from Feb 28.
2. Prove the last step of AM-GM inequality: If  $(a_1 + a_2 + \dots + a_n)/n \geq \sqrt[n]{a_1 a_2 \dots a_n}$  for every non-negative real numbers  $a_1, a_2, \dots, a_n$ , then  $\frac{a_1 + a_2 + \dots + a_{n-1}}{n-1} \geq \sqrt[n-1]{a_1 a_2 \dots a_{n-1}}$
3. Simplify the sum to a unique fraction:

$$\frac{1}{1 + \sqrt{3}} + \frac{1}{\sqrt{3} + \sqrt{5}} + \dots + \frac{1}{\sqrt{2n-1} + \sqrt{2n+1}}$$